Package: snfa (via r-universe)

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Title Smooth Non-Parametric Frontier Analysis

Version 0.0.1.9000

Description Fitting of non-parametric production frontiers for use in efficiency analysis. Methods are provided for both a smooth analogue of Data Envelopment Analysis (DEA) and a non-parametric analogue of Stochastic Frontier Analysis (SFA). Frontiers are constructed for multiple inputs and a single output using constrained kernel smoothing as in Racine et al. (2009), which allow for the imposition of monotonicity and concavity constraints on the estimated frontier.

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- Imports abind (>= 1.4.5), prodlim (>= 2018.4.18), quadprog (>= 1.5.5), rootSolve (>= 1.7)
- Suggests ggplot2 (>= 3.1.0), knitr (>= 1.20), lpSolve (>= 5.6.13), Rdpack (>= 0.10.1), rmarkdown (>= 1.10)

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allocative.efficiency Allocative efficiency estimation

Description

Fits frontier to data and estimates technical and allocative efficiency

Usage

```
allocative.efficiency(X, y, X.price, y.price, X.constrained = NA,
H.inv = NA, H.mult = 1, model = "br", method = "u",
scale.constraints = TRUE)
```

Arguments

Х	Matrix of inputs	
У	Vector of outputs	
X.price	Matrix of input prices	
y.price	Vector of output prices	
X.constrained	Matrix of inputs where constraints apply	
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb	
H.mult	Scaling factor for rule of thumb smoothing matrix	
model	Type of frontier to use; "br" for boundary regression, "sf" for stochastic frontier	
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave	
scale.constraints		
	Boolean, whether to scale constraints by their average value, can help with convergence	

allocative.efficiency

Details

This function estimates allocative inefficiency using the methodology in McKenzie (2018). The estimation process is a non-parametric analogue of Schmidt and Lovell (1979). First, the frontier is fit using either a boundary regression or stochastic frontier as in Racine et al. (2009), from which technical efficiency is estimated. Then, gradients and price ratios are computed for each observation and compared to determine the extent of misallocation. Specifically, log-overallocation is computed as

$$\log\left(\frac{w_i^j}{p_i}\right) - \log\left(\phi_i \frac{\partial f(x_i)}{\partial x^j}\right),$$

where ϕ_i is the efficiency of observation i, $\partial f(x_i)/\partial x^j$ is the marginal productivity of input j at observation i, w_i^j is the cost of input j for observation i, and p_i is the price of output for observation i.

Value

Returns a list with the following elements

y.fit	Estimated value of the frontier at X.fit	
gradient.fit	Estimated gradient of the frontier at X.fit	
technical.efficiency		
	Estimated technical efficiency	
log.overallocation		
	Estimated log-overallocation of each input for each observation	
X.eval	Matrix of inputs used for fitting	
X.constrained	Matrix of inputs where constraints apply	
H.inv	Inverse smoothing matrix used in fitting	
method	Method used to fit frontier	
scaling.factor	Factor by which constraints are multiplied before quadratic programming	

References

Aigner D, Lovell CK, Schmidt P (1977). "Formulation and estimation of stochastic frontier production function models." *Journal of econometrics*, 6(1), 21–37.

McKenzie T (2018). "Semi-Parametric Estimation of Allocative Inefficiency Using Smooth Non-Parametric Frontier Analysis." Working Paper.

Racine JEFFREYS, Parmeter CHRISTOPHERF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

Schmidt P, Lovell CK (1979). "Estimating technical and allocative inefficiency relative to stochastic production and cost frontiers." *Journal of econometrics*, **9**(3), 343–366.

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Examples

data(USMacro)

```
USMacro <- USMacro[complete.cases(USMacro),]</pre>
# Extract data
X <- as.matrix(USMacro[,c("K", "L")])</pre>
y <- USMacro$Y
X.price <- as.matrix(USMacro[,c("K.price", "L.price")])</pre>
y.price <- rep(1e9, nrow(USMacro)) #Price of $1 billion of output is $1 billion
# Run model
efficiency.model <- allocative.efficiency(X, y,
                                           X.price, y.price,
                                           X.constrained = X,
                                           model = "br",
                                           method = "mc")
# Plot technical/allocative efficiency over time
library(ggplot2)
technical.df <- data.frame(Year = USMacro$Year,</pre>
                            Efficiency = efficiency.model$technical.efficiency)
ggplot(technical.df, aes(Year, Efficiency)) +
  geom_line()
allocative.df <- data.frame(Year = rep(USMacro$Year, times = 2),
                         log.overallocation = c(efficiency.model$log.overallocation[,1],
                                                efficiency.model$log.overallocation[,2]),
                             Variable = rep(c("K", "L"), each = nrow(USMacro)))
ggplot(allocative.df, aes(Year, log.overallocation)) +
  geom_line(aes(color = Variable))
# Estimate average overallocation across sample period
lm.model <- lm(log.overallocation ~ 0 + Variable, allocative.df)</pre>
summary(lm.model)
```

dea

Data envelopment analysis

Description

Basic data envelopment analysis to replace rDEA::dea due to difficulties installing rDEA on travisci dea

Usage

dea(XREF, YREF, X, Y, model = "output", RTS = "variable")

Arguments

XREF	Matrix of inputs for observations used for constructing the frontier
YREF	Matrix of outputs for observations used for constructing the frontier
Х	Matrix of inputs for observations, for which DEA scores are estimated
Υ	Matrix of outputs for observations, for which DEA scores are estimated
model	Orientation of the model; must be "input" or "output"
RTS	Returns-to-scale for the model; must be "constant", "non-increasing" or "vari- able"

Details

This function estimates efficiency using data envelopment analysis. The linear program is constructed as in Fare et al. (1985) and optimized using lpSolve::lp. The function was built to swap with rDEA::dea because installation of rDEA presented problems for travis-ci, due to difficulties installing glpk. Should installation of rDEA on travis-ci become possible, this function will be removed.

Value

Returns a list with the following components

thetaOpt	A vector of efficiency estimates, in [0, 1] interval	
lambda	A matrix of constraint coefficients	
lambda_sum	A vector of sum of lambdas; lambda_sum = 1 for variable RTS, lambda_sum <= for non-increasing RTS	
model	Orientation of the model	
RTS	Returns-to-scale for the model	

References

Fare R, Grosskopf S, Lovell CA (1985). *The Measurement of Efficiency in Production*. Kluwer Academic Publishers.

Examples

```
# Plot technical/allocative efficiency over time
library(ggplot2)
ggplot(univariate, aes(x, y)) +
  geom_point() +
  geom_line(aes(y = frontier), color = "red")
```

fit.boundary N

Multivariate smooth boundary fitting with additional constraints

Description

Fits boundary of data with kernel smoothing, imposing monotonicity and/or concavity constraints.

Usage

```
fit.boundary(X.eval, y.eval, X.bounded, y.bounded, X.constrained = NA,
  X.fit = NA, y.fit.observed = NA, H.inv = NA, H.mult = 1,
  method = "u", scale.constraints = TRUE)
```

Arguments

X.eval	Matrix of inputs used for fitting	
y.eval	Vector of outputs used for fitting	
X.bounded	Matrix of inputs where bounding constraints apply	
y.bounded	Vector of outputs where bounding constraints apply	
X.constrained	Matrix of inputs where monotonicity/concavity constraints apply	
X.fit	Matrix of inputs where curve is fit; defaults to X.constrained	
y.fit.observed	Vector of outputs corresponding to observations in X.fit; used for efficiency calculation	
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb	
H.mult	Scaling factor for rule of thumb smoothing matrix	
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave	
scale.constrain	ts	
	Boolean, whether to scale constraints by their average value, can help with convergence	

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fit.boundary

Details

This method fits a smooth boundary of the data (with all data points below the boundary) while imposing specified monotonicity and concavity constraints. The procedure is derived from Racine et al. (2009), which develops kernel smoothing methods with bounding, monotonicity and concavity constraints. Specifically, the smoothing procedure involves finding optimal weights for a Nadaraya-Watson estimator of the form

$$\hat{y} = m(x) = \sum_{i=1}^{N} p_i A(x, x_i) y_i,$$

where x are inputs, y are outputs, p are weights, subscripts index observations, and

$$A(x, x_i) = \frac{K(x, x_i)}{\sum_{h=1}^{N} K(x, x_h)}$$

for a kernel K. This method uses a multivariate normal kernel of the form

$$K(x, x_h) = \exp\left(-\frac{1}{2}(x - x_h)'H^{-1}(x - x_h)\right),$$

where H is a bandwidth matrix. Bandwidth selection is performed via Silverman's (1986) rule-of-thumb, in the function H.inv.select.

Optimal weights \hat{p} are selected by solving the quadratic programming problem

$$\min_{p} \quad -\mathbf{1}'p + \frac{1}{2}p'p.$$

This method always imposes bounding constraints as specified points, given by

$$m(x_i) - y_i = \sum_{h=1}^N p_h A(x_i, x_h) y_h - y_i \ge 0 \quad \forall i.$$

Additionally, monotonicity constraints of the following form can be imposed at specified points:

$$\frac{\partial m(x)}{\partial x^j} = \sum_{h=1}^N p_h \frac{\partial A(x, x_h)}{\partial x^j} y_h \ge 0 \quad \forall x, j,$$

where superscripts index inputs. Finally concavity constraints of the following form can also be imposed using Afriat's (1967) conditions:

$$m(x) - m(z) \le \nabla_x m(z) \cdot (x - z) \quad \forall x, z.$$

The gradient of the frontier at a point x is given by

$$\nabla_x m(x) = \sum_{i=1}^N \hat{p}_i \nabla_x A(x, x_i) y_i,$$

where \hat{p}_i are estimated weights.

Value

Returns a list with the following elements

y.fit	Estimated value of the frontier at X.fit	
gradient.fit	Estimated gradient of the frontier at X.fit	
efficiency	Estimated efficiencies of y.fit.observed	
solution	Boolean; TRUE if frontier successfully estimated	
X.eval	Matrix of inputs used for fitting	
X.constrained	Matrix of inputs where monotonicity/concavity constraints apply	
X.fit	Matrix of inputs where curve is fit	
H.inv	Inverse smoothing matrix used in fitting	
method	Method used to fit frontier	
scaling.factor	Factor by which constraints are multiplied before quadratic programming	

References

Racine JEFFREYS, Parmeter CHRISTOPHERF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

Examples

```
data(univariate)
# Set up data for fitting
X <- as.matrix(univariate$x)</pre>
y <- univariate$y
N.fit <- 100
X.fit <- as.matrix(seq(min(X), max(X), length.out = N.fit))</pre>
# Reflect data for fitting
reflected.data <- reflect.data(X, y)</pre>
X.eval <- reflected.data$X</pre>
y.eval <- reflected.data$y</pre>
# Fit frontiers
frontier.u <- fit.boundary(X.eval, y.eval,</pre>
                             X.bounded = X, y.bounded = y,
                             X.constrained = X.fit,
                             X.fit = X.fit,
                             method = "u")
frontier.m <- fit.boundary(X.eval, y.eval,</pre>
                             X.bounded = X, y.bounded = y,
                             X.constrained = X.fit,
                             X.fit = X.fit,
                             method = "m")
```

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fit.mean

```
frontier.mc <- fit.boundary(X.eval, y.eval,</pre>
                            X.bounded = X, y.bounded = y,
                             X.constrained = X.fit,
                             X.fit = X.fit,
                             method = "mc")
# Plot frontier
library(ggplot2)
frontier.df <- data.frame(x = rep(X.fit, times = 3),</pre>
                          y = c(frontier.u$y.fit, frontier.m$y.fit, frontier.mc$y.fit),
                          model = rep(c("u", "m", "mc"), each = N.fit))
ggplot(univariate, aes(x, y)) +
 geom_point() +
 geom_line(data = frontier.df, aes(color = model))
# Plot slopes
slope.df <- data.frame(x = rep(X.fit, times = 3),</pre>
                       slope = c(frontier.u$gradient.fit,
                                  frontier.m$gradient.fit,
                                  frontier.mc$gradient.fit),
                       model = rep(c("u", "m", "mc"), each = N.fit))
ggplot(slope.df, aes(x, slope)) +
 geom_line(aes(color = model))
```

fit.mean

Kernel smoothing with additional constraints

Description

Fits conditional mean of data with kernel smoothing, imposing monotonicity and/or concavity constraints.

Usage

```
fit.mean(X.eval, y.eval, X.constrained = NA, X.fit = NA, H.inv = NA,
H.mult = 1, method = "u", scale.constraints = TRUE)
```

Arguments

X.eval	Matrix of inputs used for fitting	
y.eval	Vector of outputs used for fitting	
X.constrained	Matrix of inputs where constraints apply	
X.fit	Matrix of inputs where curve is fit; defaults to X.constrained	
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb	

H.mult	Scaling factor for rule of thumb smoothing matrix	
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave	
scale.constraints		
	Destruction to the second second state to the second second state of the second s	

Boolean, whether to scale constraints by their average value, can help with convergence

Details

This method uses kernel smoothing to fit the mean of the data while imposing specified monotonicity and concavity constraints. The procedure is derived from Racine et al. (2009), which develops kernel smoothing methods with bounding, monotonicity and concavity constraints. Specifically, the smoothing procedure involves finding optimal weights for a Nadaraya-Watson estimator of the form

$$\hat{y} = m(x) = \sum_{i=1}^{N} p_i A(x, x_i) y_i,$$

where x are inputs, y are outputs, p are weights, subscripts index observations, and

$$A(x, x_i) = \frac{K(x, x_i)}{\sum_{h=1}^{N} K(x, x_h)}$$

for a kernel K. This method uses a multivariate normal kernel of the form

$$K(x, x_h) = \exp\left(-\frac{1}{2}(x - x_h)'H^{-1}(x - x_h)\right),$$

where H is a bandwidth matrix. Bandwidth selection is performed via Silverman's (1986) rule-of-thumb, in the function H.inv.select.

Optimal weights \hat{p} are selected by solving the quadratic programming problem

$$\min_{p} \quad -\mathbf{1}'p + \frac{1}{2}p'p.$$

Monotonicity constraints of the following form can be imposed at specified points:

$$\frac{\partial m(x)}{\partial x^j} = \sum_{h=1}^N p_h \frac{\partial A(x, x_h)}{\partial x^j} y_h \ge 0 \quad \forall x, j,$$

where superscripts index inputs. Finally concavity constraints of the following form can also be imposed using Afriat's (1967) conditions:

$$m(x) - m(z) \le \nabla_x m(z) \cdot (x - z) \quad \forall x, z.$$

The gradient of the estimated curve at a point x is given by

fit.mean

$$\nabla_x m(x) = \sum_{i=1}^N \hat{p}_i \nabla_x A(x, x_i) y_i,$$

where \hat{p}_i are estimated weights.

Value

Returns a list with the following elements

y.fit	Estimated value of the frontier at X.fit
gradient.fit	Estimated gradient of the frontier at X.fit
solution	Boolean; TRUE if frontier successfully estimated
X.eval	Matrix of inputs used for fitting
X.constrained	Matrix of inputs where constraints apply
X.fit	Matrix of inputs where curve is fit
H.inv	Inverse smoothing matrix used in fitting
method	Method used to fit frontier
scaling.factor	Factor by which constraints are multiplied before quadratic programming

References

Racine JEFFREYS, Parmeter CHRISTOPHERF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

Examples

```
data(USMacro)
USMacro <- USMacro[complete.cases(USMacro),]</pre>
# Extract data
X <- as.matrix(USMacro[,c("K", "L")])</pre>
y <- USMacro$Y
# Reflect data for fitting
reflected.data <- reflect.data(X, y)</pre>
X.eval <- reflected.data$X</pre>
y.eval <- reflected.data$y</pre>
# Fit frontier
fit.mc <- fit.mean(X.eval, y.eval,</pre>
                    X.constrained = X,
                    X.fit = X,
                    method = "mc")
# Plot input productivities over time
library(ggplot2)
plot.df <- data.frame(Year = rep(USMacro$Year, times = 2),</pre>
```

fit.sf

Non-parametric stochastic frontier

Description

Fits stochastic frontier of data with kernel smoothing, imposing monotonicity and/or concavity constraints.

Usage

```
fit.sf(X, y, X.constrained = NA, H.inv = NA, H.mult = 1,
method = "u", scale.constraints = TRUE)
```

Arguments

Х	Matrix of inputs	
У	Vector of outputs	
X.constrained	Matrix of inputs where constraints apply	
H.inv	Inverse of the smoothing matrix (must be positive definite); defaults to rule of thumb	
H.mult	Scaling factor for rule of thumb smoothing matrix	
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing, and "mc" for monotonically increasing and concave	
scale.constraints		
	Boolean, whether to scale constraints by their average value, can help with convergence	

Details

This method fits non-parametric stochastic frontier models. The data-generating process is assumed to be of the form

$$\ln y_i = \ln f(x_i) + v_i - u_i,$$

where y_i is the *i*th observation of output, f is a continuous function, x_i is the *i*th observation of input, v_i is a normally-distributed error term ($v_i \sim N(0, \sigma_v^2)$), and u_i is a normally-distributed error

term truncated below at zero $(u_i \sim N^+(0, \sigma_u))$. Aigner et al. developed methods to decompose $\varepsilon_i = v_i - u_i$ into its basic components.

This procedure first fits the mean of the data using fit.mean, producing estimates of output \hat{y} . Log-proportional errors are calculated as

$$\varepsilon_i = \ln(y_i/\hat{y}_i).$$

Following Aigner et al. (1977), parameters of one- and two-sided error distributions are estimated via maximum likelihood. First,

$$\hat{\sigma}^2 = \frac{1}{N} \sum_{i=1}^N \varepsilon_i^2.$$

Then, $\hat{\lambda}$ is estimated by solving

$$\frac{1}{\hat{\sigma}^2}\sum_{i=1}^N \varepsilon_i \hat{y}_i + \frac{\hat{\lambda}}{\hat{\sigma}}\sum_{i=1}^N \frac{f_i^*}{1 - F_i^*} y_i = 0,$$

where f_i^* and F_i^* are standard normal density and distribution function, respectively, evaluated at $\varepsilon_i \hat{\lambda} \hat{\sigma}^{-1}$. Parameters of the one- and two-sided distributions are found by solving the identities

$$\sigma^2 = \sigma_u^2 + \sigma_v^2$$
$$\lambda = \frac{\sigma_u}{\sigma_v}.$$

Mean efficiency over the sample is given by

$$\exp\left(-\frac{\sqrt{2}}{\sqrt{\pi}}\right)\sigma_u,$$

and modal efficiency for each observation is given by

$$-\varepsilon(\sigma_u^2/\sigma^2).$$

Value

Returns a list with the following elements

y.fit	Estimated value of the frontier at X.fit
gradient.fit	Estimated gradient of the frontier at X.fit
mean.efficiency	,
	Average efficiency for X, y as a whole
mode.efficiency	,
	Modal efficiencies for each observation in X, y
X.eval	Matrix of inputs used for fitting

X.constrained	Matrix of inputs where constraints apply
X.fit	Matrix of inputs where curve is fit
H.inv	Inverse smoothing matrix used in fitting
method	Method used to fit frontier
scaling.factor	Factor by which constraints are multiplied before quadratic programming

References

Aigner D, Lovell CK, Schmidt P (1977). "Formulation and estimation of stochastic frontier production function models." *Journal of econometrics*, 6(1), 21–37.

Racine JEFFREYS, Parmeter CHRISTOPHERF, Du P (2009). "Constrained nonparametric kernel regression: Estimation and inference." Working paper.

Examples

```
data(USMacro)
USMacro <- USMacro[complete.cases(USMacro),]</pre>
# Extract data
X <- as.matrix(USMacro[,c("K", "L")])</pre>
y <- USMacro$Y
# Fit frontier
fit.sf <- fit.sf(X, y,</pre>
                  X.constrained = X,
                  method = "mc")
print(fit.sf$mean.efficiency)
# [1] 0.9772484
# Plot efficiency over time
library(ggplot2)
plot.df <- data.frame(Year = USMacro$Year,</pre>
                       Efficiency = fit.sf$mode.efficiency)
ggplot(plot.df, aes(Year, Efficiency)) +
  geom_line()
```

```
H.inv.select Bandwidth matrix selection
```

Description

Computes inverse of bandwidth matrix using rule-of-thumb from Silverman (1986).

H.inv.select

Usage

H.inv.select(X, H.mult = 1)

Arguments

Х	Matrix of inputs
H.mult	Scaling factor for rule-of-thumb smoothing matrix

Details

This method performs selection of (inverse) multivariate bandwidth matrices using Silverman's (1986) rule-of-thumb. Specifically, Silverman recommends setting the bandwidth matrix to

$$\begin{split} H_{jj}^{1/2} &= \left(\frac{4}{M+2}\right)^{1/(M+4)} \times N^{-1/(M+4)} \times \mathrm{sd}(x^j) \quad \text{for } j = 1, ..., M \\ H_{ab} &= 0 \quad \text{for } a \neq b \end{split}$$

where M is the number of inputs, N is the number of observations, and $sd(x^j)$ is the sample standard deviation of input j.

Value

Returns inverse bandwidth matrix

References

Silverman BW (1986). Density estimation for statistics and data analysis, volume 26. CRC press.

Examples

data(USMacro)

```
USMacro <- USMacro[complete.cases(USMacro),]
# Extract data
X <- as.matrix(USMacro[,c("K", "L")])
# Generate bandwidth matrix
print(H.inv.select(X))
#        [,1]       [,2]
# [1,] 3.642704e-08 0.000000e+00
# [2,] 0.00000e+00 1.215789e-08</pre>
```

panel.production

Description

A dataset for illustrating technical and efficiency changes using smooth non-parametric frontiers.

Usage

panel.production

Format

A data frame with 200 observations of six variables.

Firm Firm identifierYear of observationX.1 Input 1X.2 Input 2X.3 Input 3y Output

Details

Generated with the following code:

```
set.seed(100)
num.firms <- 20
num.inputs <-3
num.years <- 10</pre>
beta <- runif(num.inputs, 0, 1)</pre>
TFP.trend = 0.25
TFP <- cumsum(rnorm(num.years)) + TFP.trend * (1:num.years)</pre>
sd.measurement <- 0.05</pre>
sd.inefficiency <- 0.01</pre>
f <- function(X){</pre>
  return(TFP + X
}
gen.firm.data <- function(i){</pre>
  X = matrix(runif(num.years * num.inputs, 1, 10), ncol = num.inputs)
  y = f(X) +
    rnorm(num.years, sd = sd.measurement) -
```

reflect.data

reflect.data

Data reflection for kernel smoothing

Description

This function reflects data below minimum and above maximum for use in reducing endpoint bias in kernel smoothing.

Usage

reflect.data(X, y)

Arguments

Х	Matrix of inputs
у	Vector of outputs

Value

Returns a list with the following elements

X.reflected	Reflected values of X
y.reflected	Reflected values of y

Examples

```
data(univariate)
```

```
# Extract data
X <- as.matrix(univariate$x)
y <- univariate$y
# Reflect data
reflected.data <- reflect.data(X, y)
X.reflected <- reflected.data$X</pre>
```

```
y.reflected <- reflected.data$y</pre>
```

technical.efficiency.change

Technical and efficiency change estimation

Description

Estimates technical and efficiency change using SNFA

Usage

```
technical.efficiency.change(df, input.var.names, output.var.name,
  firm.var.name, time.var.name, method = "u")
```

Arguments

df	Data frame with variables used in estimation
<pre>input.var.names</pre>	S
	Names of input variables; must appear in df
output.var.name	9
	Name of output variable; must appear in df
firm.var.name	Name of firm variable; must appear in df
time.var.name	Name of time variable; must appear in df
method	Constraints to apply; "u" for unconstrained, "m" for monotonically increasing and "mc" for monotonically increasing and concave

Details

This function decomposes change in productivity into efficiency and technical change, as in Fare et al. (1994), using smooth non-parametric frontier analysis. Denoting $D_s(x_t, y_t)$ as the efficiency of the production plan in year t relative to the production frontier in year s, efficiency change for a given firm in year t is calculated as

$$\frac{D_{t+1}(x_{t+1}, y_{t+1})}{D_t(x_t, y_t)},$$

and technical change is given by

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$$\left(\frac{D_t(x_{t+1}, y_{t+1})}{D_{t+1}(x_{t+1}, y_{t+1})} \times \frac{D_t(x_t, y_t)}{D_{t+1}(x_t, y_t)}\right)^{1/2}.$$

Value

Returns a data.frame with the following columns

firm.var.name	Column of firm name data	
time.var.name	Column of time period data	
efficiency.change		
	Average annual efficiency change since the previous period in data	
technical.change		
	Average annual technical change since the previous period in data	
productivity.change		
	Average annual productivity change since the previous period in data	

References

Fare R, Grosskopf S, Norris M, Zhang Z (1994). "Productivity Growth, Technical Progress, and Efficiency Change in Industrialized Countries." *The American Economic Review*, **84**(1), 66-83.

Examples

univariate

Description

A dataset for illustrating univariate non-parametric boundary regressions and various constraints.

Usage

univariate

Format

A data frame with 50 observations of two variables.

x Input

y Output

Details

Generated with the following code:

USMacro

US Macroeconomic Data

Description

A dataset of real output, labor force, capital stock, wages, and interest rates for the U.S. between 1929 and 2014, as available. All nominal values converted to 2010 U.S. dollars using GDP price deflator.

Usage

USMacro

USMacro

Format

A data frame with 89 observations of four variables.

Year Year

Y Real GDP, in billions of dollars

K Capital stock, in billions of dollars

K.price Annual cost of \$1 billion of capital, using 10-year treasury

L Labor force, in thousands of people

L.price Annual wage for one thousand people

Source

https://fred.stlouisfed.org/

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